

Slope And Distance

1 Find Δx and Δy for this pair of coordinates.

$$\begin{array}{ll}
 P1(0, 5) & P2(4, -3) \\
 \Delta x = x_2 - x_1 & \Delta y = y_2 - y_1 \\
 = 4 - 0 & = -3 - 5 \\
 \Delta x = 4 & \Delta y = -8
 \end{array}$$

2 Find Δx and Δy for this pair of coordinates.

$$\begin{array}{ll}
 P1(-2, -4) & P2(3, -1) \\
 \Delta x = x_2 - x_1 & \Delta y = y_2 - y_1 \\
 = 3 - (-2) & = -1 - (-4) \\
 \Delta x = 5 & \Delta y = 3
 \end{array}$$

3 Given two points, if $\Delta x = 6$ and $\Delta y = 12$, what is the slope of the line they form?

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{12}{6} = 2$$

4 Given two points, if $\Delta x = 3$ and $\Delta y = -1$, what is the slope of the line they form?

$$\text{slope} = \frac{\Delta y}{\Delta x} = \frac{-1}{3} \text{ or } -0.\bar{3}$$

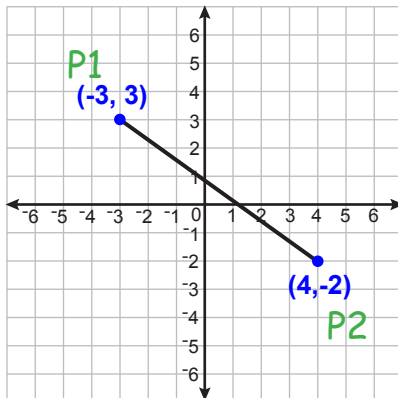
5 Given two points, if $\Delta x = 5$ and $\Delta y = -4$, what is the distance between them?

$$\begin{aligned}
 d &= \sqrt{(\Delta x)^2 + (\Delta y)^2} = \sqrt{(5)^2 + (-4)^2} \\
 &= \sqrt{25 + 16} \\
 &= \sqrt{41} \text{ or } 6.403
 \end{aligned}$$

6 Given two points, if $\Delta x = -1$ and $\Delta y = -7$, what is the distance between them?

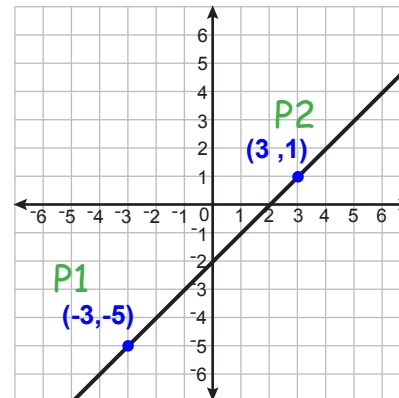
$$\begin{aligned}
 d &= \sqrt{(\Delta x)^2 + (\Delta y)^2} = \sqrt{(-1)^2 + (-7)^2} \\
 &= \sqrt{1 + 49} \\
 &= \sqrt{50} \text{ or } 5\sqrt{2} \\
 &\text{ or } 7.071
 \end{aligned}$$

7 Find the slope of this line segment, and the distance between its two end points.



$$\begin{array}{ll}
 \Delta x = 4 - (-3) & \text{slope} = \frac{-5}{7} \text{ or } 0.714 \\
 \Delta x = 7 & \\
 \Delta y = -2 - 3 & \\
 \Delta y = -5 & \\
 d = \sqrt{(7)^2 + (-5)^2} & \\
 = \sqrt{49 + 25} & \\
 = \sqrt{74} \text{ or } 8.602 &
 \end{array}$$

8 Find the slope of this line, and the distance between the two points shown.



$$\begin{array}{ll}
 \Delta x = 3 - (-3) & \text{slope} = \frac{6}{6} = 1 \\
 \Delta x = 6 & \\
 \Delta y = 1 - (-5) & \\
 \Delta y = 6 & \\
 d = \sqrt{(6)^2 + (6)^2} & \\
 = \sqrt{36 + 36} & \\
 = \sqrt{72} \text{ or } 6\sqrt{2} & \\
 \text{ or } 8.485 &
 \end{array}$$