The Distributive Property Pattern

TDP 1

Instructions: The Distributive Property pattern shows two equivalent forms of an expression involving a factor multiplied by a group. In these problems, if you are given the grouped form, then use the Distributive Property to re-write the expression without the group. But if you are given the distributed form, then apply the Distributive Property in reverse to "factor out" the common factor. See examples:

grouped form	distributed form

$$1 a(b+c) = ab + ac$$

$$2(x-y) = 2x-2y$$

$$5(a-b) =$$

$$= ax + ay$$

$$4(a+b-c) =$$

$$= xa + xb + xc$$

$$= yx^2 + yx$$

$$9 \quad -2(a+b+c) =$$

$$= (-3x) + (-3y)$$

$$2(5a + 5b) =$$

$$= 5x + 10y$$

Applying the Distributive Property - Set 1

TDP 2

Instructions: Apply the Distributive Property to eliminate the group in each expression.

$$4(2x+10)$$

$$5(a + 2b)$$

$$4(2x) + 4(10)$$

$$8x + 40$$

$$-2(x+1)$$

$$-3(x-1)$$

$$a(a+b+c)$$

$$x(x^2-x-1)$$

$$3(2x + b + 6c)$$

$$-1(5x-2y+7z)$$

$$2x(y+4)$$

$$x^2(x-1)$$

$$-a(a-2b)$$

$$3x(4x + 5y)$$

Applying the Distributive Property - Set 2

TDP 3

Instructions: Apply the Distributive Property to eliminate the group in each expression.

$$-5(5x^2 + x - 2)$$

$$y(3y + 5)$$

$$(-5)(5x^2) + (-5)(x) + (-5)(-2)$$

-25x² - 5x + 10

$$-3(x^2-5)$$

$$b(3a - 4b + c)$$

$$9(x + ax + 10)$$

$$4x(x^2-y^2)$$

$$-x^2(x+y-1)$$

$$6(2x - 5y + 4z)$$

$$y = xy(x + y)$$

$$5(-a^3 - 2a^2 + 1)$$

$$-2(-2x-3y-4z)$$

Identifying Common Factors

TDP 4

Instructions: In order to apply the Distributive Property in reverse, you need to be able to identify factors that are common to each term in a polynomial. You can only factor something out if it's a factor of every term. For each polynomial, list any factors that all of its terms have in common. (If there are no common factors, write "none")

common factors

$$2x^2 + 6x + 4$$

$$3a^3 + 3a^2 + 3a$$

3a

$$bx + by -bz$$

$$\frac{4}{3}$$
 5a - 10b - 20c

$$axy + bxc - yzx$$

$$x^6 + x^4 + x^2$$

$$3a - 6b - 12c$$

$$9$$
 ay + by + bc

$$-2x + (-2y) + (-2z)$$

-2x + (-2y) + (-2z)

$$-4x^2 + 8x + 16$$

$$6x^3 + 2x^2 - 4x$$

"Factoring Out" - Set 1

TDP 5

Instructions: Look at each polynomial to identify the common factor(s) in each term. Then, use the Distributive Property in reverse to factor them out.

$$6x + 24$$

$$6(x) + 6(4)$$

$$6(x + 4)$$

$$2x^2 + 20$$

$$5 3x^2 + 3y^2 + 3$$

$$9 (-7)a^2 + (-7)b^2$$

$$-xy - 2xz$$

$$5a^2 - 10a$$

$$5a(a) - 5a(2)$$

$$5a(a - 2)$$

$$4a - 4b - 4c$$

$$2xy - 2xz$$

$$5x + 40y + 25$$

$$3x^3 - 6x^2 - 9x$$

"Factoring Out" - Set 2

TDP 6

Instructions: Look at each polynomial to identify the common factor(s) in each term. Then, use the Distributive Property in reverse to factor them out.

$$2x^2 + 2x + 6$$

$$2(x^2) + 2(x) + 2(3)$$

$$2(x^2 + x + 3)$$

$$5x^2 + 5x + 5$$

$$ax + ay^2 + az$$

$$\boxed{4x + 16y}$$

$$9 7a^2 + 7ab$$

$$x^3 + x^2 - x$$

$$x(x^2) + x(x) - x(1)$$

$$x(x^2 + x - 1)$$

$$\frac{1}{4}$$
 $3a - 6b - 9c$

$$\boxed{6} \quad 2ax + 2ay + 2az$$

$$-5x - 5y$$

$$-2x + (-4y) + (-6z)$$

$$-x^3 - x^2 - x$$